# DIFFERENTIAL EQUATIONS AND LAPLACE TRANSFORMS 

(Common to all branches)
[As per Choice Based Credit System (CBCS) scheme]
(From the academic year 2021-22)

|  | Course Code | 21 MA21 | CIE Marks | 50 |
| :--- | :--- | :--- | :--- | :--- |
|  | Credits | 03 | SEE Marks | 50 |
|  | Contact Hours/Week (L-T-P) | $3-0-0$ | Total Marks | 100 |
|  | Contact Hours | 42 | Exam Hours | 03 |

Course Learning Objectives: This course (21MA21) will enable students to master the basic tools of differential \& integral calculus, differential equations and elementary linear algebra and become skilled for solving problems in science and engineering.

## MODULE-I

Ordinary differential equations(ODE's)of first order:-
8 Hours
Linear and reducible to linear differential equation. Exact and reducible to exact differential equations. Applications of ODE's-orthogonal trajectories, Newton's law of cooling and L-R circuits. Nonlinear differential equations; introduction to general and singular solutions; solvable for p only; Clairaut's and reducible to Clairaut's equations only.
RBT Levels: L1, L2 \& L3

## MODULE-II

Ordinary Differential Equations (ODE's) of higher order:-
Differential equation of higher order with constant coefficients and examples. Second order linear ODE's with constant coefficients by the method of variation of parameters; Cauchy's and Legendre homogeneous differential equations. Initial and boundary value problems. Applications to oscillations of a spring and L-C-R circuits.
RBT Levels: L1, L2 \& L3

## MODULE-III

## Partial Differential Equations(PDE's):-

## 9 Hours

Formation of PDE's by elimination of arbitrary constants and arbitrary functions. Solution of non-homogeneous PDE by direct integration method. Homogeneous PDEs involving derivative with respect to one independent variable only. Solution of PDE's by the method of separation of variable.

## Application of Partial Differential Equations(PDE's):-

Introduction, derivation of one dimensional wave equation and heat equation, various possible solutions of one dimensional wave equation and heat equation and Laplace equation by the method of separation variables and examples.
RBT Levels: L1, L2 \& L3

## MODULE-IV

## Vector Calculus:-

8 Hours
Vector Differentiation: Scalar and vector fields. Gradient, directional derivative; divergence and curl physical interpretation; solenoidal and irrotational vector fields- Illustrative problems.
Vector Integration: Line integrals, Greens Theorem, Gauss Divergence Theorem and Stokes Theorem (Only Statements) Illustrative examples. Applications to work done by a force and flux. RBT Levels: L1, L2 \& L3

## MODULE-V

## Laplace Transformations:

## 8 Hours

Defination, Transforms of elementary functions. Laplace transform of Derivatives and integrals and problems, periodic function and Unit step function- Illustrative problems. Inverse Laplace transforms, properties - Illustrative problems, Solution of linear differential equations.
RBT Levels: L1, L2 \& L3

## Text Books:

1. B.S. Grewal: Higher Engineering Mathematics, Khanna Publishers, $43^{\text {rd }}$ Ed.,2015.
2. E. Kreyszig: Advanced Engineering Mathematics, John Wiley \& Sons, $10^{\text {th }}$ Ed.(Reprint), 2016.

## Reference books:

1. Early Transcendental Calculus- James Stewart, Thomson Books, 5e 2007
2. N.P.Bali and Manish Goyal: A Text Book of Engineering Mathematics, Laxmi Publishers, $7^{\text {th }}$ Ed., 2010.
3. B.V.Ramana: "Higher Engineering Mathematics" $11^{\text {th }}$ Edition, Tata McGraw-Hill, 2010.
4. Veerarajan T.," Engineering Mathematics for First year", Tata McGraw-Hill, 2008.
5. Thomas G.B. and Finney R.L."Calculus and Analytical Geometry" $9^{\text {th }}$ Edition, Pearson,

## E-Books and Online resources:

- http://.ac.in/courses.php?disciplineID=111
- http://www.class-central.com/subject/math(MOOCs)
- http://academicearth.org/


## Pedagogy (General Instructions):

These are sample Strategies, which teachers can use to accelerate the attainment of the various course outcomes.

1. In addition to the traditional lecture method, different types of innovative teaching methods may be adopted so that the delivered lessons shall develop student's theoretical and applied mathematical skills.
2. State the need for Mathematics with Engineering Studies and Provide real-life examples
3. Support and guide the students for self-study.
4. You will also be responsible for assigning homework, grading assignments and quizzes, and documenting students' progress.
5. Encourage the students for group learning to improve their creative and analytical skills.
6. Show short related video lectures in the following ways:

- As an introduction to new topics (pre-lecture activity).
- As a revision of topics (post-lecture activity).
- As additional examples (post-lecture activity).
- As an additional material of challenging topics (pre-and post-lecture activity).
- As a model solution of some exercises (post-lecture activity).

Course Outcomes: On completion of this course, students are able to:
CO1: Explain various physical models through first order and first degree ordinary differential equations and solve them by analytically
CO2: Explain various physical models through second and higher order ordinary differential equations and solve them analytically
CO3: Understand a variety of partial differential equations and solution by exact methods and apply methods of separation of variables to solve heat, wave, laplace equations.
CO4: Illustrate the applications vector calculus to understand the solenoidal and irrotational vectors and also to exhibit the interdependence of line, surface and volume integrals.
CO5: Apply the knowledge of Laplace transform and inverse Laplace transform to solve the differential equations.

|  | PO1 | PO2 | PO3 | PO4 | PO5 | PO6 | PO7 | PO8 | PO9 | PO10 | PO11 | PO12 |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  | CO1 | 3 | 1 |  |  |  |  |  |  |  |  |  | 1 |
|  | CO2 | 3 | 1 |  |  |  |  |  |  |  |  |  | 1 |
| CO3 | 3 | 2 |  |  |  |  |  |  |  |  |  | 1 |  |
| CO4 | 3 | 1 |  |  |  |  |  |  |  |  |  | 1 |  |
| CO5 | 3 | 1 |  |  |  |  |  |  |  |  |  | 1 |  |
|  | AVG | 3 | 1.2 |  |  |  |  |  |  |  |  |  | 1 |

## Method of Examination:

Note:- The SEE question paper will be set for 100 marks and the marks scored by the student will be proportionately reduced to 50 .

- The question paper will have ten full questions carrying equal marks.
- Each full question carries 20marks.
- There will be two full questions (with a maximum of four sub questions) from each module.
- Each full question will have sub question covering all the topics under a module.

The students will have to answer five full questions, selecting one full question from each module.

